

# Multistep Approach for Optimizing Design and Operation of the C-Town Pipe Network Model

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**Abstract:** A multiobjective approach is used here to optimize design and operation of the C-Town pipe network, searching for trade-off solutions between (1) installation cost, (2) operational cost, and (3) cost of the pressure-reducing valves. Due to the large number of decisional variables and to the complexity of the constraints considered, the optimization problem was tackled in five steps: (1) identification of some feasible (on the basis of the many constraints) first attempt solutions; (2) application of a multiobjective genetic algorithm to the 2D optimization problem with objective functions 1 and 2, in order to obtain optimal trade-off solutions between the installation cost and operational cost, without considering the installation of pressure-reducing valves; (3) application of the multiobjective genetic algorithm to the optimization problem with objective functions 2 and 3 for each of the solution selected at the end of Step 2, in order to assess how the operational cost can decrease thanks to the installation and operation of pressure-reducing valves; (4) derivation of the 3D Pareto surface by grouping the solutions found at the end of Steps (2) and (3). A solution was extracted from the 3D Pareto surface of optimal solutions following some specific criteria. This solution was then further refined (Step 5) in order to allow for variable settings of the pressure-reducing valves installed and to make it compliant with the battle guidelines concerning leakage modeling. DOI: 10.1061/(ASCE)WR.1943-5452.0000585. © 2015 American Society of Civil Engineers.

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## Introduction

Water distribution systems require frequent upgrades and interventions during their useful life in order to keep up with urban extension and population growth. Other upgrades are also needed to reduce the occurrence of pipe bursts and the amount of leakage. Overall, the interventions in a network can be grouped into three categories:

1. Design, related to network construction or expansion;
2. Maintenance, aimed at attenuating pipe breaks and leakage; and
3. Actuator regulation, aimed at searching for the most suitable settings of the regulators (such as pumps and valves) installed in the network, in order to dynamically adjust the network itself to spatial and temporal demand variations.

These three categories of interventions should be carried out simultaneously in order to guarantee maximization of the overall network operational efficiency.

Optimization techniques proposed in the scientific literature can be used to assist water-utility managers in selecting and prioritizing the interventions to be made (Alperovits and Shamir 1977; Jowitt and Xu 1990; Quimpo and Shamsi 1991; Ormsbee and Lansey 1994; Simpson et al. 1994; Arulraj and Rao 1995; Alvisi and Franchini 2006; Alvisi and Franchini 2009; Campisano et al. 2010;

and Creaco and Franchini 2012; Alvisi and Franchini 2013; Creaco and Franchini 2013; Alvisi and Franchini 2014; Creaco et al. 2014b). These listed papers do represent valid contributions to the field but have the drawback of focusing only on one category of interventions at a time: i.e., design (Alperovits and Shamir 1977; Simpson et al. 1994; Creaco and Franchini 2012; Alvisi and Franchini 2014; Creaco et al. 2014), maintenance (Quimpo and Shamsi 1991; Arulraj and Rao 1995, Alvisi and Franchini 2006; Alvisi and Franchini 2009; Alvisi and Franchini 2013), or actuator regulation (Jowitt and Xu 1990; Quimpo and Shamsi 1991; Campisano et al. 2010; Creaco and Franchini 2013).

Unlike the simpler case studies usually dealt with in the scientific literature, the optimization problem proposed in the context of BBLAWN is closer to water utility managers' reality, since it involves design, maintenance, and actuator-regulation aspects at the same time. A new methodology was then developed to tackle the multiple facets of this optimization problem.

## BBLAWN Optimization Problem and Its Simplification

The case study of the BBLAWN is the C-Town network, made up of

- $n_0 = 1$  reservoir;
- $n_t = 7$  tanks;
- $n = 388$  nodes with unknown heads;
- $n_p = 432$  pipes;
- $n_{pu} = 11$  pumps grouped in 5 pumping stations; and
- 1 throttle valve.

The network is subdivided into  $n_{dis} = 5$  districts, each of which featuring a pumping system and a system of tanks (actually a single tank for all the districts except for Districts 1 and 5 where two tanks are present). The operation of each district can be summed up in two loading conditions: (1) district and associated tank fed by the district pumping system, and (2) pumping system off and district

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74 fed by its system of tanks. District pumping stations are numbered  
 75 like the districts. As benchmark of the network operation, a series  
 76 of 7 days (168 h), scanned with a 1-h-long time step, was consid-  
 77 ered. An accurate description of the optimization problem of the  
 78 BBLAWN is present in the work of Giustolisi et al. (2015).

79 The objective space of the optimization is made up of three  
 80 functions: (1) installation cost  $C_i$ , related to the laying of new pipes  
 81 plus the widening of the tanks plus the insertion of new pumps;  
 82 (2) operational cost  $C_o$ , obtained as the sum of the yearly pumping  
 83 cost and the monetized value of the yearly leakage volume; (3) cost  
 84  $C_v$  of the pressure-reducing valves (PRVs) installed in the network  
 85 in order to lower the service pressure and then attenuate leakage.

86 The decisional variables can be grouped as follows:

- 87 • Subgroup (1): Diameters of the new pipes that can be installed at  
 88 the various pipe sites to replace the old leaky pipes or in parallel  
 89 to the latter (size  $2n_p$ );
- 90 • Subgroup (2): Tank-widening volumes (size  $n_t$ );
- 91 • Subgroup (3): Pumps that can be used to replace the old  
 92 pumps of low efficiency, or can be laid in parallel to them (size  
 93  $n_{pu} + n_{dis}$ );
- 94 • Subgroup (4): Positions of the isolation valves that can be closed  
 95 in the network in order to create, inside each district, subdis-  
 96 tricts whose service pressure can be easily regulated by means  
 97 of pressure-reducing valves (size  $2n_p$  because, theoretically,  
 98 an isolation valve could be inserted in each pipe and in its par-  
 99 allel pipe);
- 100 • Subgroup (5): Positions and settings (initially assumed as fixed)  
 101 of the PRVs to be installed in the network (size  $2n_p$  because,  
 102 theoretically, a PRV could be installed in each pipe and in its  
 103 parallel pipe);
- 104 • Subgroup (6): Switch on and off settings of the various  
 105 pumps, and open and closed setting of the throttle valve [size  
 106  $2 \times (n_{pu} + n_{dis} + 1)$ ].

107 According to this classification, the total number of decisional  
 108 variables is then equal to  $6n_p + n_t + 3n_{pu} + 3n_{dis} + 2 = 2,649$ .

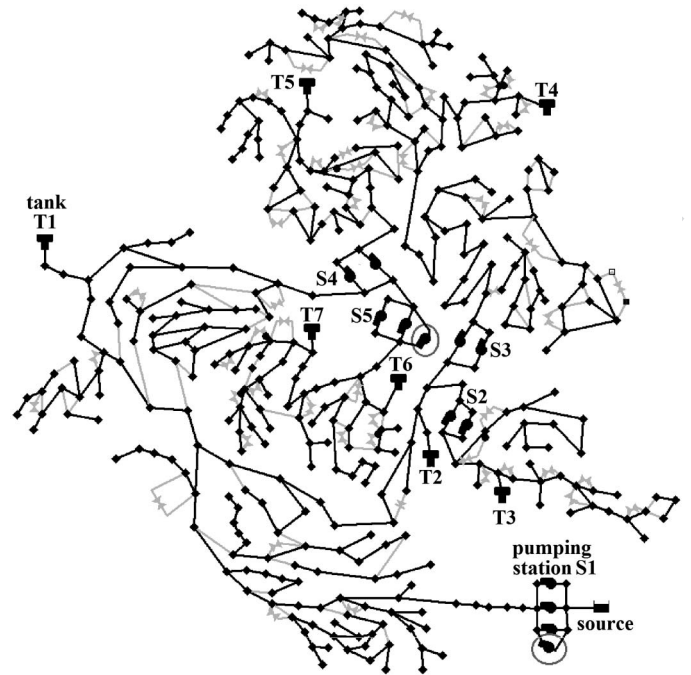
109 In order to simplify the research space, some assumptions  
 110 were made:

- 111 • Simplification 1: No parallel pipes were allowed, since laying  
 112 parallel pipes has the drawback of increasing network length  
 113 and then leakage;
- 114 • Simplification 2: Following engineering judgment, laying  
 115 pumps in parallel was allowed for only in Pumping Stations  
 116 1 and 5 (Fig. 1);
- 117 • Simplification 3: The potential positions of the isolation valves  
 118 to be closed and of the PRVs to be installed were identified a  
 119 priori thanks to the algorithm proposed by Creaco and Pezzinga  
 120 (2014, 2015) and on the basis of engineering judgment. Overall,  
 121 64 potentially closed isolation valves and 51 potentially in-  
 122 stalled PRVs were identified (Fig. 1).

123 Simplification 1 makes the size of Subgroup 1 equal to  
 124  $n_p = 432$ .

125 Simplification 2 makes the size of Subgroup 3 equal to  $n_{pu} +$   
 126  $2 = 13$  and the size of Subgroup 6 equal to 28.

127 As far as Simplification 3 is concerned, some comments deserve  
 128 to be made about the algorithm proposed by Creaco and Pezzinga  
 129 (2014, 2015) and its application to the C-Town network. This al-  
 130 gorithm is hybrid, being based on the coupling of a multiobjective  
 131 genetic algorithm [NSGAI (Deb et al. 2002)] and of an algorithm  
 132 based on the iterated linear programming [upgraded version of that  
 133 presented by Jowitt and Xu (1990)]. The genetic algorithm enables  
 134 optimal location of the control valves as well as identification of the  
 135 isolation valves that have to be closed, with the objective to simul-  
 136 taneously minimize leakage volumes and control valve costs. The  
 137 algorithm based on iterated linear programming is embedded in the



**Fig. 1.** C-Town network; in grey the pipes where an isolation valve can be closed and the potential location of PRVs (these valves are here shown in parallel to their location with an attempt to be better identified); grey circles show the two locations where new pumps can be installed in parallel in Stations 1 and 5

138 genetic algorithm and searches for the optimal settings of the control  
 139 valves for each solution proposed by the genetic algorithm,  
 140 made up of a set of isolation valves closed and control valves in-  
 141 stalled in the network. The algorithm of Creaco and Pezzinga  
 142 (2014, 2015) was applied to each of the  $n_{dis} = 5$  districts of the  
 143 BBLAWN network at a time, considering the two different loading  
 144 conditions previously described.

145 Overall, Simplification 3 makes the sizes of Subgroups 4 and 5  
 146 equal to 64 and 102, respectively.

147 Thanks to the previous simplifying assumptions, the total num-  
 148 ber of decisional variables was then reduced to 646.

149 The constraints of the optimization include

- 150 • Constraint 1: Continuity equations for network nodes and tanks;
- 151 • Constraint 2: Momentum equations for network pipes, pumps,  
 152 and valves;
- 153 • Constraint 3: Minimum pressure head requirements for the  
 154 various network nodes (see the BBLAWN guidelines); and
- 155 • Constraint 4: Tank levels at the end of the operational period,  
 156 which have to be larger than or equal to their respective initial  
 157 levels.

158 Whereas Constraints 1 and 2 were automatically respected in  
 159 the present study thanks to the use of the hydraulic simulator  
 160 EPANET2 (Rossman 2000), the respect of Constraints 3 and 4 was  
 161 obtained through adoption of penalties in the objective functions.

162 In the following sections, first the optimization algorithm used  
 163 to explore the 3D research space is described and applied. Then, the  
 164 choice and refinement of the final solution taken out from the 3D  
 165 Pareto surface are explained.

## 166 Optimization Algorithm

167 As shown in the previous section, the optimization problem of  
 168 BBLAWN is very complex since it simultaneously concerns pipe

169 replacements, pump replacements and additions, pump settings,  
 170 tank upgrades, isolation valve closures and, finally, PRV installations  
 171 and regulations. A decoupling strategy (Creaco et al. 2014a)  
 172 was then adopted in this study, in a bid to simplify the problem. In  
 173 particular, this strategy consisted in splitting the problem in various  
 174 stages. In particular, the following steps were then carried out using  
 175 the software EPANET2 (Rossman 2000) for network simulation:

- 176 1. Identification of some feasible first attempt solutions;
- 177 2. Optimization with Objective Functions 1 (installation cost)  
 178 and 2 (operational cost: energy cost plus water-loss cost);
- 179 3. Optimization with Objective Functions 2 (operational cost)  
 180 and 3 (cost of the pressure-reducing valves);
- 181 4. Approximation of the 3D Pareto surface; and
- 182 5. Refinement of a final solution selected within the 3D Pareto  
 183 surface obtained in Step 4.

184 In the following subsections, these steps are thoroughly  
 185 described.

### 186 Step 1

187 In this step, engineering judgment was used to implement some  
 188 variations in the network asset and in pump settings in order to  
 189 obtain some first-attempt solutions with no PRVs (and then with  
 190  $C_v = 0$ ) in the trade-off between Objective Function 1 ( $C_i$ ) and  
 191 Objective Function 2 ( $C_o$ ). In particular, seven first-attempt  
 192 solutions were obtained in this step:

- 193 • Two solutions with very low values of  $C_i$  (around  $5 \times 10^4$  Euro)  
 194 and quite high values of  $C_o$  (slightly lower than  $2 \times 10^6$  Euro).  
 195 In these solutions, very small variations were made from the  
 196 initial layout, which enabled the network to respect the pressure  
 197 constraints, including replacement of some pipes in the original  
 198 layout and variations in pump settings;
- 199 • Four solutions with intermediate values of  $C_i$  and  $C_o$ , close to  
 200  $3 \times 10^5$  and  $1.6 \times 10^6$  Euro, respectively. These solutions were  
 201 obtained by replacing pipes mainly in the lines which intercon-  
 202 nect pumps and tanks, enlarging tanks T4 and T5, closing some  
 203 network pipes in order to create some districts, and manually  
 204 fixing the pump settings; and
- 205 • One solution with a very high value of  $C_i$  (around  $7.2 \times 10^5$   
 206 Euro) and quite low value of  $C_o$  (around  $5.2 \times 10^5$  Euro). This  
 207 solution was obtained by replacing pipes in the whole network,  
 208 enlarging tanks T4 and T5, closing a large number of pipes in  
 209 order to create many districts, and manually fixing the pump  
 210 settings.

211 These solutions, whose values of  $C_i$  and  $C_o$  are reported in the  
 212 graph in Fig. 2, made it possible to get an initial idea of the range of  
 213 values taken by the first two objective functions.

### 214 Step 2

215 The objective of this step was to explore the trade-off between  
 216 Objective Function 1 ( $C_i$ ) and objective Function 2 ( $C_o$ ), while ne-  
 217 glecting the effects of the installation of PRVs. To this end, a 2D  
 218 optimization was performed using the multiobjective genetic algo-  
 219 rithm NSGAI (Deb et al. 2002) and considering a population of  
 220 200 individuals and a total number of 400 generations. The first  
 221 attempt solutions detected in Step 1 were inserted in the initial pop-  
 222 ulation in order to accelerate the convergence of the NSGAI  
 223 towards feasible solutions. The decisional variables considered in  
 224 Step 2 were those belonging to the Subgroups 1, 2, 3, 4, and 6  
 225 presented in the section entitled “BBLAWN optimization problem  
 226 and its simplification.”

227 At the end of the 400 generations, a 2D Pareto front of optimal  
 228 solutions featuring  $C_v = 0$  was obtained. Then, 10 solutions well

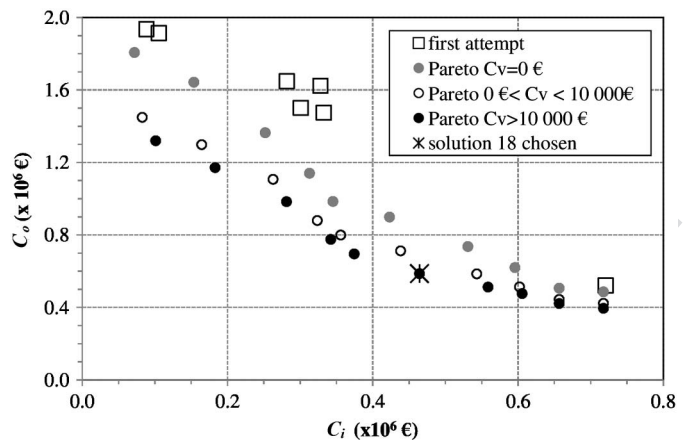


Fig. 2. First-attempt solutions and solutions of the 3D Pareto surface;  
 end solution chosen

scattered over the whole range of values of the objective function  
 values were taken out from this front and reported in the graph in  
 Fig. 2. As an example, one of these solutions is Solution 19 featur-  
 ing values  $C_i = 531,126$  Euro and  $C_o = 736,699$  Euro. The effi-  
 ciency and effectiveness of the Step 2 optimization is proven by the  
 fact that the solutions of the 2D Pareto front dominate by far the  
 first attempt solutions assumed in Step 1.

### Step 3

This step was aimed at exploring the trade-off between Objective  
 Function 3 ( $C_v$ ) and Objective Function 2 ( $C_o$ ) starting from the  
 asset of each of the 10 solutions selected at the end of Step 2.  
 To this end, other 2D optimizations (one for each of the 10 solu-  
 tions) were performed using the multiobjective genetic algorithm  
 NSGAI (Deb et al. 2002) and considering a population of 50 indi-  
 viduals and a total number of 100 generations. The decisional var-  
 iables considered in Step 3 were those belonging to the Subgroups  
 4, 5, and 6 presented in section 2. During each optimization, an  
 artifice was adopted to enable reduction in the total cost  $C_v$  of in-  
 stalled PRVs. This artifice consisted in replacing the generic pipe  
 where PRV installation is encoded with a new pipe featuring the  
 smallest diameter and, then, the lowest PRV cost.

At the end of the generic Step 3 optimization, a Pareto front of  
 optimal solution in the space  $C_v$ - $C_o$  was obtained for the generic  
 of the 10 asset solutions selected at the end of Step 2. In each Step 3  
 Pareto front, the solution with the lowest  $C_v$  value (i.e.,  $C_v = 0$ )  
 coincided with the starting Step 2 solution. From each Step 3 Pareto  
 front, two solutions were taken out:

- Solution 1: Solution with an intermediate  $C_v$  value, correspond-  
 ing to an intermediate number of valves installed in the network;
- Solution 2: Solution with the highest  $C_v$  value, corresponding to  
 the highest number of valves installed in the network.

As example of the extracted solutions from the 2D Pareto fronts  
 of Step 3, there are Solutions 20 and 21, which were obtained  
 from the optimization carried out starting from Solution 19 of  
 Step 2. These solutions feature  $C_v$  equal to 6,783 and 14,418 Euro,  
 respectively.

### Step iv

The objective functions values of the two solutions selected from  
 each of the Step 3 Pareto fronts in Step 3 were reported in the graph  
 in Fig. 2 along with those obtained at the end of Step 2. Three

different colors were used in the figure to differentiate the solutions on the basis of the  $C_v$  value. As a result of this, an approximation of the Pareto surface, which is made up of 30 solutions and represents the trade-off between the three objective functions, was obtained. For each of these solutions, the objective function values are also reported in the following Table 1, along with the partial rank in terms of each of the objective functions and the total rank obtained as the sum of the solution partial ranks. Finally, Table 1 reports, for each solution, the total yearly cost  $C_{tot}$ , obtained as the sum of the three objective functions, which are all expressed as yearly costs.

For the selection of the final solution in the 3D Pareto surface, two different criteria, related to the minimum rank and to the minimum cost respectively, could be applied. The first criterion would lead to selection of either Solution 27 or Solution 30, which have the lowest rank equal to 30. The second would lead, instead, to selection of Solution 18, which features the lowest value of the total cost  $C_{tot}$ . In the end, Solution 18 was chosen as end solution because Solutions 27 and 30 were deemed to be exceedingly extreme, and then unacceptable to water utility managers, since they would require replacement of all network pipes. Furthermore, Solution 18 is not much worse than Solutions 27 and 30 in terms of total rank (32 instead of 30).

As shown in Fig. 3(a), Solution 18 encodes replacement of all the pipes in District 1 (fed by pumping station 1). In the other districts, pipe replacements concern the paths that link the pumping stations to the tanks and the PRV sites. As shown in Fig. 3(b), Solution 18 also encodes the closure of the isolation valves in some network pipes and the permanent switch-off of some pumps. No pump replacements and additions are encoded in Solution 18 and tank extension only concerns tank T5.

A proof of the effectiveness of the optimization is provided in the graphs in Fig. 4, which report the flow supplied by pumping station S2 and the water level in tank T3 fed by S2, respectively. These graphs, selected as representative and illustrative of the operation of pumping stations and network tanks, show that the optimization process was able to create a daily cyclic profile for pumped flows and water-tank levels. This profile was achieved through the search for proper pump settings, which causes pumps to operate mainly at night time, when energy costs are lower.

### Step v

Solution 18 selected at the end of Step 4 was refined in Step 5. In particular, this process included two different refinements:

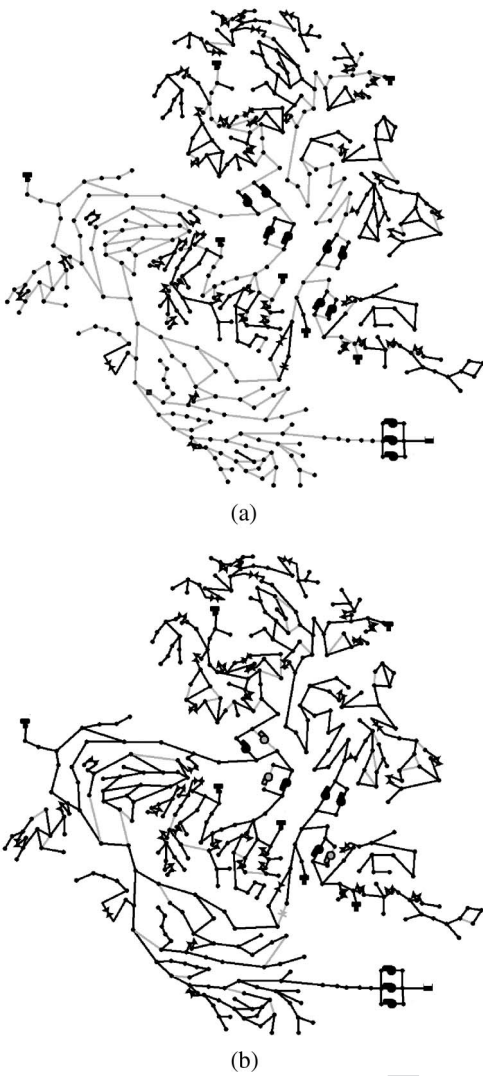
- Refinement 1: Determination of time-varying settings for the pressure head to be imposed downstream of PRVs;
- Refinement 2: Transformation of leakage modeling from the Tucciarelli et al. (1999) formulation, easily obtained in EPANET2 by means of the nodal emitters, to the Germanopoulos (1985) formulation, which is compliant with the BBLAWN guidelines (Giustolisi et al. 2015).

Both refinements determine no variations in the network asset of Solution 18, and then in the values of  $C_i$  and  $C_v$ . In fact, they are only expected to change leakage and, then,  $C_o$ .

In order to accomplish Refinement 1, the critical node (i.e., the node with the lowest pressure head) was identified downstream of each PRV installed in the network. The EPANET2 results relative to this node enabled calculation of the excess of pressure head compared to the minimum requirement at each time instant of operation. At each time instant, the downstream target pressure head of

**Table 1.** For Each Solution of the 3D Pareto Surface, ID, Values of the Objective Functions  $C_i$ ,  $C_o$ , and  $C_v$  and of Total Cost  $C_{tot}$  Ranked in Terms of Each Objective Function and Total Rank

Identifier solution	$C_i$ (Euro)	$C_o$ (Euro)	$C_v$ (Euro)	$C_{tot}$ (Euro)	$C_i$ rank	$C_o$ rank	$C_v$ rank	Total rank	
T1:1	1	72-(177)	1,806-(742)	0	1,878-(918)	1	30	1	32
T1:2	2	82-(979)	1,449-(744)	6-(783)	1,539-(506)	2	28	2	32
T1:3	3	101-(470)	1,319-(473)	14-(668)	1,435-(611)	3	26	4	33
T1:4	4	153-(885)	1,643-(264)	0	1,797-(149)	4	29	1	34
T1:5	5	164-(687)	1,297-(958)	6-(783)	1,469-(428)	5	25	2	32
T1:6	6	183-(178)	1,171-(792)	14-(668)	1,369-(637)	6	24	4	34
T1:7	7	252-(278)	1,364-(167)	0	1,616-(445)	7	27	1	35
T1:8	8	263-(080)	1,107-(292)	6-(783)	1,377-(155)	8	22	2	32
T1:9	9	281-(571)	983-(825)	14-(668)	1,280-(064)	9	20	4	33
T1:10	10	313-(079)	1,140-(553)	0	1,453-(632)	10	23	1	34
T1:11	11	323-(881)	879-(923)	6-(783)	1,210-(587)	11	18	2	31
T1:12	12	342-(372)	775-(156)	14-(668)	1,132-(196)	12	16	4	32
T1:13	13	345-(320)	985-(540)	0	1,330-(861)	13	21	1	35
T1:14	14	356-(123)	799-(591)	6-(783)	1,162-(497)	14	17	2	33
T1:15	15	374-(613)	695-(880)	14-(668)	1,085-(161)	15	13	4	32
T1:16	16	423-(459)	898-(393)	0	1,321-(852)	16	19	1	36
T1:17	17	438-(690)	711-(645)	6-(783)	1,157-(118)	17	14	2	33
T1:18	18	464-(520)	586-(898)	14-(418)	1,065-(836)	18	11	3	32
T1:19	19	531-(126)	736-(699)	0	1,267-(825)	19	15	1	35
T1:20	20	543-(514)	585-(412)	6-(783)	1,135-(709)	20	10	2	32
T1:21	21	558-(844)	512-(451)	14-(418)	1,085-(713)	21	9	3	33
T1:22	22	595-(870)	620-(012)	0	1,215-(883)	22	12	1	35
T1:23	23	602-(320)	513-(736)	6-(783)	1,122-(840)	23	8	2	33
T1:24	24	605-(881)	476-(541)	14-(418)	1,096-(840)	24	5	3	32
T1:25	25	657-(014)	506-(471)	0	1,163-(485)	25	7	1	33
T1:26	26	657-(014)	444-(426)	6-(783)	1,108-(223)	25	4	2	31
T1:27	27	657-(014)	421-(396)	14-(418)	1,092-(828)	25	2	3	30
T1:28	28	717-(786)	486-(171)	0	1,203-(957)	26	6	1	33
T1:29	29	717-(786)	422-(714)	6-(783)	1,147-(283)	26	3	2	31
T1:30	30	717-(786)	395-(452)	14-(418)	1,127-(657)	26	1	3	30
T1:32	18 refined	464-(520)	580-(842)	14-(418)	1,059-(780)	—	—	—	—



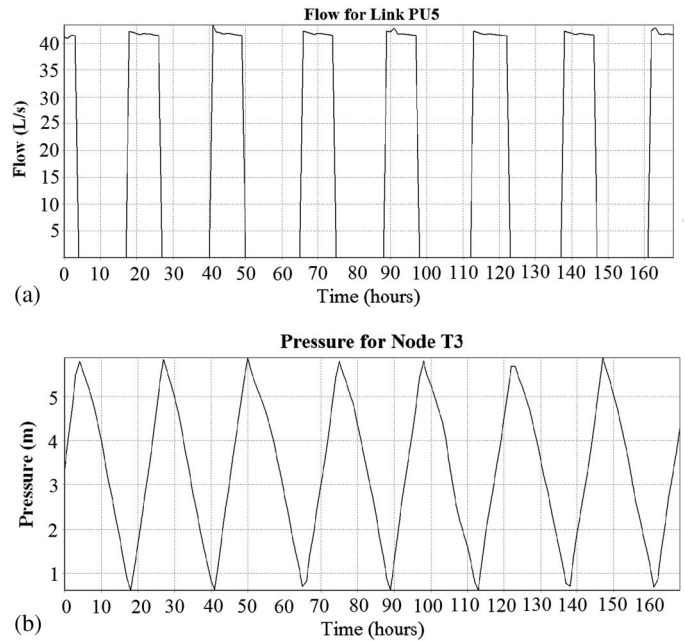
**Fig. 3.** Solution 18: (a) in grey, pipes replaced in the network; (b) in grey, pipes where the isolation valve is closed and permanently-switched-off pumps

each PRV was then reduced in order to lead the critical-node pressure head excess to 0. This refinement virtually enables a far control node to be considered for each PRV, instead of the node placed immediately downstream. As a result of this refinement, a slight reduction in  $C_o$  from 586,898 to 583,670 Euro was obtained.

Refinement 2 was carried out in order to express leakage through the Germanopoulos (1985) formulation, which assumes the generic pipe leakage to be calculated as a function of the average pressure head at the pipe's end nodes and then to be allocated to the pipe end-nodes themselves.

In order to obtain the Germanopoulos (1985) formulation for Solution 18, EPANET2 was run iteratively according to the following stages, which refer to the generic network operation time instant:

- Stage 0: A starting distribution of network nodal pressures is considered (a good first attempt distribution is represented by the distribution obtained through the EPANET2 run with the emitters). The application of a suitably set up MATLAB subroutine enables evaluation of pipe leakages on the basis of the Germanopoulos (1985) formulation;
- Stage 1: Pipe leakages evaluated in the previous phase are stored in memory;



**Fig. 4.** Solution 18; (a) water discharge pumped by pump PU5; (b) water level in Tank T3

- Stage 2: Pipe leakages are allocated to the network nodes;
- Stage 3: An EPANET2 input file of the network is constructed where, for each node, a variation in the total demand (users' demand + allocated leakage) is allowed (by means of patterns);
- Stage 4: EPANET2 is run; a distribution of network nodal pressures is obtained. The application of the MATLAB subroutine enables evaluation of pipe leakages on the basis of Germanopoulos (1985) formulation;
- Stage 5: The absolute differences between pipe leakages in Stage 4 and those of Stage 2 are calculated. If the maximum absolute difference is below a certain tolerance threshold, convergence on pipe leakages evaluated on the basis of the Germanopoulos (1985) formulation has been reached. Otherwise the procedure continues from Stage 1.

The application of Refinement 2 only slightly changed the operational cost  $C_o$  from 583,670 to 580,842 Euro. This small variation proves that the Tucciarelli et al. (1999) formulation, used throughout the optimizations, approximates very well the Germanopoulos (1985) formulation required by the BBLAWN guidelines. As a result of this, the overall methodology adopted in this work, based on the adoption of the Tucciarelli et al. (1999) formulation for the representation of leakage, is legitimated.

## Conclusions

This work showed how the design and operation of a real and complex network can be optimized using a multistep approach that combines engineering judgment and optimizations. In particular, following the search for first-attempt solutions obtained through application of engineering judgment, an optimization process with three objective functions [(1) installation cost, (2) operational cost, and (3) cost of the pressure-reducing valves] was carried out. For the sake of simplification, this process was split into subsequent 2D optimizations, where the trade-off between installation cost and operational cost was first explored, followed by that between cost of pressure-reducing valves and operational cost. After an approximated 3D Pareto surface was obtained, a criterion based on the

384 minimum total cost, obtained as the sum of installation, opera- 427  
 385 tional, and valve costs, was conveniently used for selecting the 428  
 386 **ultimate** solution. At the end of the applications, the benefits de- 429  
 387 rived from adopting, for each pressure-reducing valve, a far control 430  
 388 node instead of the node placed immediately downstream, were 431  
 389 investigated. Since this variation was made available by the organ- 432  
 390 izers of the battle without extra installation costs, it was profitably 433  
 391 implemented in the **end** solution, in light of the subsequent slight 434  
 392 decrease in the operational cost. However, in real case studies, the 435  
 393 implementation of this option could require extra costs related to 436  
 394 the installation of real time control devices, which then need to be 437  
 395 compromised with the benefits in an ad hoc financial analysis. 438

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 403 [comunicazione/la-brochure-dei-tecnopoli](http://fesr.regione.emilia-romagna.it/allegati/comunicazione/la-brochure-dei-tecnopoli)). 445

## 404 References

405 Alperovits, E., and Shamir, U. (1977). “Design of optimal water distribu- 446  
 406 tion systems.” *Water Resour. Res.*, 13(6), 885–900. 447  
 407 Alvisi, S., and Franchini, M. (2006). “Near optimal rehabilitation schedul- 448  
 408 ing of water distribution systems based on a multiobjective genetic 449  
 409 algorithm.” *Civ. Eng. Environ. Syst.*, 23(3), 143–160. 450  
 410 Alvisi, S., and Franchini, M. (2009). “Multiobjective optimization of 451  
 411 rehabilitation and leakage detection scheduling in water distribution 452  
 412 systems.” *J. Water Resour. Plann. Manage.*, 10.1061/(ASCE)0733- 453  
 413 9496(2009)135:6(426), 426–439. 454  
 414 Alvisi, S., and Franchini, M. (2013). “A heuristic procedure for the auto- 455  
 415 matic creation of district metered areas in water distribution systems.” 456  
 416 *Urban Water J.*, 11(2), 137–159. 457  
 417 Alvisi, S., and Franchini, M. (2014). “Water distribution systems: Using 458  
 418 linearized hydraulic equations within the framework of ranking-based 459  
 419 optimization algorithms to improve their computational efficiency.” 460  
 420 *Environ. Modell. Software*, 57, 33–39. 461  
 421 Arulraj, G. P., and Rao, H. S. (1995). “Concept of significance index for 462  
 422 maintenance and design of pipe networks.” *J. Hydraul. Eng.*, 10.1061/ 463  
 423 (ASCE)0733-9429(1995)121:11(833), 833–837. 464  
 424 Campisano, A., Creaco, E., and Modica, C. (2010). “RTC of valves for 465  
 425 leakage reduction in water supply networks.” *J. Water Resour. Plann. 466*  
 426 *Manage.*, 10.1061/(ASCE)0733-9496(2010)136:1(138), 138–141. 467

Creaco, E., Alvisi, S., and Franchini, M. (2014a). “A multi-step approach 427  
 for optimal design and management of the C-Town pipe network 428  
 model.” *Procedia Eng.*, 89, 37–44. 429  
 Creaco, E., and Franchini, M. (2012). “Fast network multi-objective de- 430  
 sign algorithm combined with an a posteriori procedure for reliability 431  
 evaluation under various operational scenarios.” *Urban Water J.*, 9(6), 432  
 385–399. 433  
 Creaco, E., and Franchini, M. (2013). “A new algorithm for the real time 434  
 pressure control in water distribution networks.” *Water Sci. Technol.* 435  
*Water Supply*, 13(4), 875–882. 436  
 Creaco, E., Franchini, M., and Walski, T. M. (2014b). “Accounting 437  
 for phasing of construction within the design of water distribution 438  
 networks.” *J. Water Resour. Plann. Manage.*, 10.1061/(ASCE)WR 439  
 .1943-5452.0000358, 598–606. 440  
 Creaco, E., and Pezzinga, G. (2014). “Embedding linear programming in 441  
 multi objective genetic algorithms for reducing the size of the search 442  
 space with application to leakage minimization in water distribution 443  
 networks.” *Environ. Modell. Software*, 444  
 Creaco, E., and Pezzinga, G. (2015). “Multi-objective optimization of pipe 445  
 replacements and control valve installations for leakage attenuation 446  
 in water distribution networks.” *J. Water Resour. Plann. Manage.*, 447  
 10.1061/(ASCE)WR.1943-5452.0000458, 04014059-1-04014059-10. 448  
 Deb, K., Pratap, A., Agarwal, S., and Meyarivan, T. (2002). “A fast and 449  
 elitist multiobjective genetic algorithm: NSGA-II.” *IEEE Trans. Evol. 450*  
*Comput.*, 6(2), 182–197. 451  
 Germanopoulos, G. (1985). “A technical note on the inclusion of pressure 452  
 dependent demand and leakage terms in water supply network models.” 453  
*Civ. Eng. Syst.*, 2(3), 171–179. 454  
 Giustolisi, O., Berardi, L., Laucelli, D., Savic, D., and Kapelan, Z. (2015). 455  
 “Operational and tactical management of water and energy resources 456  
 in pressurized systems: The competition at WDSA 2014.” *J. Water 457*  
*Resour. Plann. Manage.*, 458  
 Jowitt, P. W., and Xu, C. (1990). “Optimal valve control in water distribu- 459  
 tion networks.” *J. Water Resour. Plann. Manage.*, 10.1061/(ASCE) 460  
 0733-9496(1990)116:4(455), 455–472. 461  
 Ormsbee, L. E. and Lansey, K. E. (1994). “Optimal control of water supply 462  
 pumping systems.” *J. Water Resour. Plann. Manage.*, 10.1061/(ASCE) 463  
 0733-9496(1994)120:2(237), 237–252. 464  
 Quimpo, R. G., and Shamsi, U. M. (1991). “Reliability-based distribution 465  
 system maintenance.” *J. Water Resour. Plann. Manage.*, 10.1061/ 466  
 (ASCE)0733-9496(1991)117:3(321), 321–339. 467  
 Rossman, L. A. (2000). “EPANET 2 users manual.” Environmental Protec- 468  
 tion Agency. 469  
 Simpson, A. R., Dandy, G. C., and Murphy, L. J. (1994). “Genetic 470  
 algorithms compared to other techniques for pipe optimization.” 471  
*J. Water Resour. Plann. Manage.*, 10.1061/(ASCE)0733-9496(1994) 472  
 120:4(423), 423–443. 473  
 Tucciarelli, T., Criminisi, A., and Termini, D. (1999). “Leak analysis in 474  
 pipeline system by means of optimal value regulation.” *J. Hydraul. 475*  
*Eng.*, 10.1061/(ASCE)0733-9429(1999)125:3(277), 277–285. 476