

# Book of Abstract

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## **Characterisation of Crack/Notch Tip Fields**

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## 7<sup>th</sup> of June (Day 3)

### Session VIII – Chairman: Thierry Palin-Luc

- 9.00-9.20 **Aleksandar Sedmak, Srdja Perkovic, Zijah Burzic, Zoran Radakovic.**  
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- 9.20-9.40 **Giovanni Meneghetti, Alberto Visentin, Alberto Campagnolo.**  
*Implementation of the Peak Stress Method for the automated FEA-assisted design of welded structures subjected to variable amplitude multiaxial fatigue loads ..... p. 43*
- 9.40-10.00 **Paolo Livieri, Roberto Tovo.**  
*Review of the design fatigue strength for steel butt welded joints: influence of geometrical factors and shape defects ..... p. 33*
- 10.00-10.20 **Paolo Livieri.**  
*Simplified analysis of stress intensity factors at weld toe ..... p. 31*
- 10.20-10.50 Coffee break

### 10.50-11.50 Discussion Session & Closure – Chairman: Michael Vormwald & Youshi Hong

## End of Day 3

## Simplified analysis of stress intensity factors at weld toe

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The J-integral is a path-independent integral introduced by Rice [1] and Cherepanov [2], that established a simple relationship between the path integral and the stress intensity factors (SIF) of a crack subjected to mode I, mode II and mode III loadings. Successively, Chiarelli and Frediani [3] and Huber et al. [4] considered the extension from a 2D to 3D model by considering an integral in a plane perpendicular to the crack front starting from Eshelby’s energy momentum tensor.

The J-integral applied to a V-notch in a plate (namely  $J_V$ ) is not constant if the initial and final integration points are moved along the side but the path independence of the integral is always verified. If we consider a path with fixed points at each end at the same distance  $\rho$  from the origin (see Figure 1), the  $J_V$  assume a simplified formulation [5,6]:

$$J_V = J_{V1} + J_{V2} + J_{V3} = \bar{J}_1 \frac{K_{N,1}^2}{E'} \rho^{2\lambda_1-1} + \bar{J}_2 \frac{K_{N,2}^2}{E'} \rho^{2\lambda_2-1} + \bar{J}_3 \frac{K_{N,3}^2}{2G} \rho^{2\lambda_3-1} \quad (1)$$

where  $K_N$  are the notch stress intensity factors,  $\bar{J}_i$  are parameters that only depend on the opening angle  $2\alpha$ ,  $E'$  is equal to the elastic modulus  $E$  for plane stress and  $E'=E/(1-\nu^2)$  for plane strain, and  $G$  is the shear modulus. Furthermore, each  $J_V$  mode is proportional to the corresponding mode (I, II or III) of the classic  $J_i$  integral of a virtual embedded crack lying along the bisector of the V-notch and with a length equal to  $\rho$  (see Figure 2):

$$\frac{J_i \Big|_a}{J_{V,i} \Big|_{r=\rho}} = v_i \quad i = 1, 2, 3 \quad (2)$$

The parameters  $v_i$  are reported in Table 1 for an opening angle of 135 degrees. So that, the stress intensity factors of a crack behind a sharp V-notch can be calculated by means of the  $J_V$  evaluated for the V-notch without modelling the crack with the same external load and boundary conditions. Table 3 reports the values of  $v_i$  for a selected opening angle.

The aim of this paper is to verify the use of the  $J_V$  integral in welded structures for the evaluations of the stress intensity factors of a crack at the weld toe by means of the three-dimensional FE model without modelling the crack. Figure (2) shows a hollow section subjected to tensile loading ( $F$ ) and torque ( $M_t$ ). The opening angle is of 135 degrees. When the size of the weld toe tends to zero, accurate FE analysis show that the  $v_i$  parameters tend to that reported in table 1. Figure 2 shows the trend of  $v_i$ .

**Table 1.**  $v_i$  parameters for an opening angle of 135 degrees

$2\alpha$	$v_1$	$v_2$	$v_3$
135°	1.74	2.12	1.23

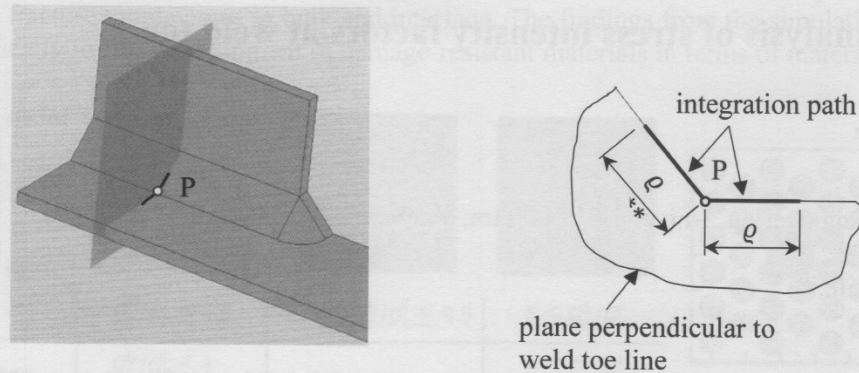


Figure 1.  $J_V$  for a welded joint with a sharpe V-notch.

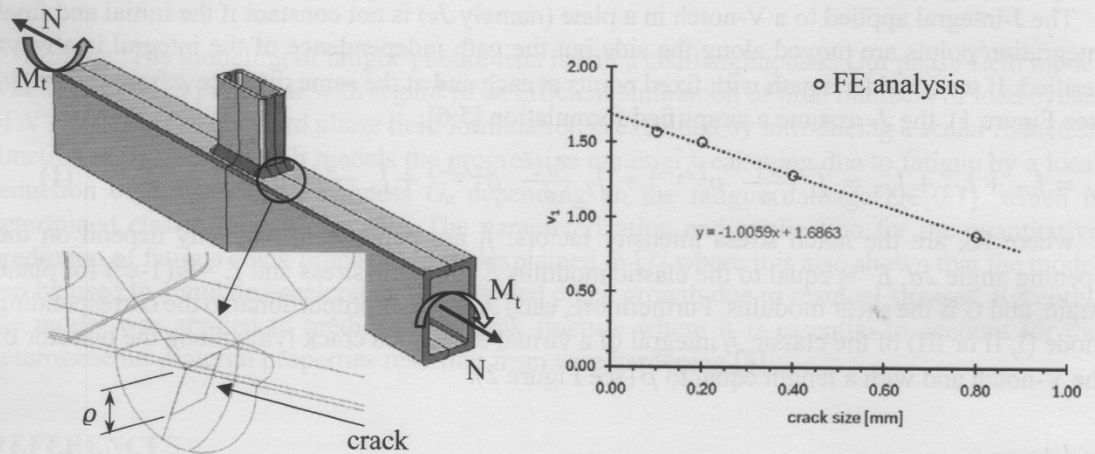


Figure 2. Value of the parameter  $\nu_l$  at the weld toe obtained with a three-dimensional FE analysis.

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