## Precise Measurement of the $e^+e^- \rightarrow D_s^{*+}D_s^{*-}$ Cross Sections at Center-of-Mass Energies from Threshold to 4.95 GeV

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The process  $e^+e^- \rightarrow D_s^{*+}D_s^{*-}$  is studied with a semi-inclusive method using data samples at center-ofmass energies from threshold to 4.95 GeV collected with the BESIII detector operating at the Beijing Electron Positron Collider. The Born cross sections of the process are measured for the first time with high precision in this energy region. Two resonance structures are observed in the energy-dependent cross sections around 4.2 and 4.4 GeV. By fitting the cross sections with a coherent sum of three Breit-Wigner amplitudes and one phase-space amplitude, the two significant structures are assigned masses of (4186.8 ±  $8.7 \pm 30$ ) and (4414.6 ±  $3.4 \pm 6.1$ ) MeV/ $c^2$ , widths of (55 ± 15 ± 53) and (122.5 ± 7.5 ± 8.1) MeV, where the first errors are statistical and the second ones are systematic. The inclusion of a third Breit-Wigner amplitude is necessary to describe a structure around 4.79 GeV.

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In  $e^+e^-$  annihilations, several conventional vector charmonium states are established in the inclusive hadronic cross sections above the open charm threshold, such as the  $\psi(3770)$ ,  $\psi(4040)$ ,  $\psi(4160)$ , and  $\psi(4415)$ . However, unexpected vector charmoniumlike resonance structures have also been discovered over the past two decades with a charmonium and light hadrons in the final state. These include  $\psi(4230)$ , initially observed in the  $e^+e^- \rightarrow \pi^+\pi^- J/\psi$  process [1,2], and  $\psi(4360)$  and  $\psi(4660)$ , initially observed in  $e^+e^- \rightarrow \pi^+\pi^-\psi(3686)$  [3,4] by the *B*factory experiments *BABAR* and Belle.

These vector charmonium(-like) states have been searched for or further investigated experimentally in many decay modes, involving charmonium states (such as  $\pi^+\pi^-J/\psi$  [5],  $K\bar{K}J/\psi$  [6,7],  $\eta J/\psi$  [8,9],  $\eta' J/\psi$  [10],  $\pi\pi h_c$  [11–13],  $\pi^+\pi^-\psi(3686)$  [14], and  $\omega\chi_{cJ}$  [15]), and charmed mesons (such as  $D\bar{D}$  [16,17],  $D^{*0}D^{*-}\pi^+ + \text{c.c.}$  [18] and  $\bar{D}D^*\pi + \text{c.c.}$  [19]), whereas experimental results of the decay modes involving charmed strange mesons are inadequate. Interestingly, the mass of the  $\psi(4230)$  state lies just at the production threshold of the  $D_s^{*+}D_s^{*-}$  pair.

The measurements of the exclusive cross sections for charmed strange meson pairs were performed by CLEO-c at center-of-mass energies ( $E_{c.m.}$ ) up to 4.26 GeV [20], and by *BABAR* [21] and Belle [22] with the initial-state radiation (ISR) method. Since these results are limited by either energy range (CLEO-c) or statistics (*BABAR* and Belle), it could not be concluded yet whether these vector

charmonium(-like) states decay into charmed strange meson pairs or not.

With the data samples taken by the BESIII experiment, the cross sections of  $e^+e^- \rightarrow D_s^{*+}D_s^{*-}$  can be measured from the production threshold up to 4.95 GeV, with much improved precision over previous experiments. This unique measurement allows to investigate the vector chamonium(-like) structures, therefore shedding light on their nature.

The BESIII detector is described in detail in [23,24]. The experimental data used in this analysis were taken at  $E_{c.m.}$  ranging from 4.226 GeV (just above the  $D_s^{*+}D_s^{*-}$  production threshold) to 4.95 GeV with 76 energy points [25–27] corresponding in total to an integrated luminosity of 15.67 fb<sup>-1</sup> [27–29]. A Geant4-based [30] Monte Carlo (MC) package, which includes the geometric description of the BESIII detector and its response, is used to produce simulated samples which are used to estimate the backgrounds and to determine the detection efficiencies and ISR corrections.

The  $e^+e^- \rightarrow D_s^{*+}D_s^{*-}$  events are generated using helicity-amplitude (HELAMP) models in EvtGen [31,32] at all the energy points, where the HELAMP inputs (relative magnitudes of the helicity amplitudes) are extracted from the helicity angular distributions of data, the width of  $D_s^{*\pm}$  is set to zero, and beam energy spread and ISR are considered with the generator KKMC [33,34]. Possible background contributions are estimated with inclusive MC samples generated by KKMC with integrated luminosities comparable to data, in which the known decay modes are modeled with EvtGen using branching fractions taken from the Particle Data Group [35], and the remaining unknown charmonium decays are modeled with LUNDCHARM [36]. Final-state radiation (FSR) from charged particles is incorporated by the PHOTOS package [37].

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To increase efficiency, a semi-inclusive method is performed by reconstructing only  $D_s^{*+}$  or  $D_s^{*-}$  of  $e^+e^- \rightarrow D_s^{*+}D_s^{*-}$ , with  $D_s^{*\pm} \rightarrow \gamma D_s^{\pm} \rightarrow \gamma K^+ K^- \pi^{\pm}$ . With this method at least one good photon, one pair of  $K^+K^-$ , and one  $\pi^{\pm}$  are required in the final state. The selection criteria for charged tracks and photon candidates are described in Ref. [38]. To select  $D_s^{\pm}$  candidates, the invariant mass  $m_{KK\pi}$  of  $K^+K^-\pi^{\pm}$  is required to be in the range  $|m_{KK\pi} - m_{D_s}| < 15 \text{ MeV}/c^2$ , where  $m_{D_s}$  is the nominal  $D_s^{\pm}$  mass [35]. All the  $\gamma D_s^{\pm}$  (i.e.  $\gamma K^+ K^- \pi^{\pm}$ ) combinations are taken as  $D_s^{*\pm}$  candidates for further selection. As the missing mass  $m_{\rm miss}$  and the invariant mass  $m_{\gamma K K \pi}$  of  $D_s^{*\pm} \rightarrow \gamma K^+ K^- \pi^{\pm}$  candidates are anticorrelated, a modified missing mass  $M_{\rm miss} \equiv m_{\rm miss} + m_{\gamma KK\pi}$  $m_{D_s^*}$  is used to improve the resolution, where  $m_{D_s^*}$  is the nominal mass of  $D_s^{*\pm}$  [35]. With the signal MC events, the resolution of  $M_{\text{miss}}$  is estimated and parametrized as an energy dependent function  $\sigma_{M_{\text{miss}}}^{\text{MC}}(E_{\text{c.m.}})$ . To select  $D_s^{*\pm}$ from  $e^+e^- \rightarrow D_s^{*+}D_s^{*-}$  events and suppress background, the modified missing mass of  $D_s^{*\pm}$  candidates is required to be in a window  $|M_{\text{miss}} - m_{D_s^*}| < 5\sigma_{M_{\text{miss}}}^{\text{MC}}(E_{\text{c.m.}})$ . Because of the positive correlation between  $m_{\gamma KK\pi}$  and  $m_{KK\pi}$ , a modified mass  $M_{\gamma KK\pi} \equiv m_{\gamma KK\pi} - m_{KK\pi} + m_{D_s}$  is used for  $D_s^{*\pm}$  candidates to improve the resolution.

The yield of  $D_s^{*\pm}$  signals is determined by fitting the  $M_{\gamma KK\pi}$  distributions. To describe the  $D_s^{*\pm}$  signal shape in data, the  $M_{\gamma KK\pi}$  shape of correct  $\gamma KK\pi$  combinations from  $e^+e^- \rightarrow D_s^{*+}D_s^{*-}$  MC, which is figured out by matching the MC truth, is used. This MC signal shape is convolved with a Gaussian function to take into account the possible mass shift  $\Delta m$ , and the resolution (and  $D_s^*$  width) difference  $\Delta \sigma$  between data and MC simulation. The  $M_{\gamma KK\pi}$  shape of random  $\gamma KK\pi$  combinations from  $e^+e^- \rightarrow D_s^{*+}D_s^{*-}$  MC is also used as one component and its ratio relative to the one for correct combinations is fixed according to the MC study. To describe the background in  $M_{\gamma KK\pi}$  distribution for data, a second order Chebyshev function  $1 + c_0 x + c_0 x$  $c_1(2x^2-1)$  with two coefficients  $c_0$  and  $c_1$  is used. The parameters  $\Delta m$ ,  $\Delta \sigma$ ,  $c_0$ , and  $c_1$  are floating initially in the fits. Since no  $E_{\rm c.m.}$  dependence is observed for  $\Delta m$ ,  $\Delta \sigma$ , and  $c_1$ , they are finally fixed to the values averaged over  $E_{c.m.}$  in the fits to determine the nominal  $D_s^{*\pm}$  signal yields, leaving only  $c_0$  as floating. As an example, the fit of  $M_{\gamma K K \pi}$  to data at  $E_{\text{c.m.}} = 4.29 \text{ GeV}$  [39] is shown in Fig. 1.

A study of the inclusive MC samples shows that no peaking background is found from events without  $D_s^{\pm\pm}$  after applying all the selection criteria. The ISR-produced  $D_s^{\pm}D_s^{\mp\mp}$  events can contribute as a peaking background, which is subtracted by normalized MC according to the cross sections of  $e^+e^- \rightarrow D_s^{\pm}D_s^{\mp\mp}$  [40] and the luminosities. The other two-body processes containing  $D_s^{\pm\pm}$  are  $e^+e^- \rightarrow D_s^{\pm\pm}D_{sJ}^{(*)\mp}$ , but they fail the missing mass



FIG. 1. The  $M_{\gamma KK\pi}$  distribution for data at 4.29 GeV. The black curve represents the fit, the red dashed curve the background, the blue dot-dashed curve the random combinations of  $\gamma KK\pi$  from  $e^+e^- \rightarrow D_s^{*\pm}D_s^{*\mp}$ , and the blue dashed curve the correct  $\gamma KK\pi$  combinations from the signal.

requirement. For the same reason, the three-body process  $e^+e^- \rightarrow D_s^*D^{(*)}K$  does not contribute as peaking backgrounds either. The contribution from the three-body process  $e^+e^- \rightarrow D_s^{*\pm}D_s^{\mp}\pi^0$  is expected to be negligible due to isospin violation and the missing mass requirement.

The Born cross section  $\sigma_{\text{Born}}$  and the dressed cross section  $\sigma_{\text{dressed}}$  at each energy point are calculated using

$$\begin{split} \sigma_{\text{Born}} &= \sigma_{\text{dressed}} |1 - \Pi|^2 \\ &= \frac{N_{D_s^*}^{\text{fit}} - N_{D_s^{\pm} D_s^{\mp \mp}}}{2\mathcal{B}(D_s^{\pm} \to K^+ K^- \pi^{\pm})\epsilon(1 + \delta) \frac{1}{|1 - \Pi|^2} \mathcal{L}_{\text{int}}}, \quad (1) \end{split}$$

where  $N_{D_s^*}^{\text{fit}}$  is the fitted  $D_s^*$  signal yield,  $N_{D_s^{\pm}D_s^{*\mp}}$  is the number of the estimated peaking background events from the ISR produced  $D_s^{\pm}D_s^{*\mp}$ ,  $\mathcal{L}_{\text{int}}$  is the integrated luminosity,  $1 + \delta$  is the ISR correction factor,  $(1/|1 - \Pi|^2)$  is the correction factor from the vacuum polarization (VP) [41],  $\mathcal{B}(D_s^{\pm} \to K^+K^-\pi^{\pm})$  is the branching fraction of the decay  $D_s^{\pm} \to K^+K^-\pi^{\pm}$ , which is taken from Ref. [35], and  $\epsilon$  is the detection efficiency times the branching fraction of  $D_s^{*\pm} \to$  $\gamma D_s^{\pm}$  [35]. As  $D_s^{*+}$  and  $D_s^{*-}$  are not separated in the fitted signal yields, there is a factor of 2 in the denominator.

The ISR effect also impacts on the detection efficiency in addition to the correction factor. Since ISR depends on the dressed cross section line shape, an iterative procedure is used to determine the dressed cross sections [42]. First, signal MC samples are generated at all the energy points with a flat dressed cross section line shape using KKMC to determine the initial detection efficiencies, ISR correction factors and subsequently the preliminary measured dressed cross sections are fitted with a coherent sum of three Breit-Wigner (BW) and one two-body phase-space (PHSP) amplitudes assuming  $D_s^{*+}D_s^{*-}$  in *P* wave [43]



FIG. 2. Three fitting results for the measured dressed cross sections of  $e^+e^- \rightarrow D_s^{*+}D_s^{*-}$ . The black dots with error bars are for the measured dressed cross sections. In each plot, the black curve represents the fit; the green dashed, blue two-dashed, and red long-dashed ones are for the three BW amplitudes from the fit, respectively, and the pink dot-dashed is for the PHSP contributions.

$$\sigma_{\text{dressed}} = \left| BW_1(E_{\text{c.m.}}) + \sum_{j=2}^3 BW_j(E_{\text{c.m.}})e^{i\phi_j} + \frac{a_0\sqrt{\beta^3(E_{\text{c.m.}})}}{E_{\text{c.m.}}^n}e^{i\phi_0} \right|^2,\tag{2}$$

where

$$BW_{1}(E_{\text{c.m.}}) = \frac{M_{1}}{E_{\text{c.m.}}} \cdot \frac{B_{1}(E_{\text{c.m.}})\sqrt{12\pi a_{1}\Gamma_{1}}}{E_{\text{c.m.}}^{2} - M_{1}^{2} + iM_{1}\Gamma_{1}} \cdot \sqrt{\beta^{3}(E_{\text{c.m.}})}$$
(3)

is the first BW amplitude [44],

$$BW_{j}(E_{\text{c.m.}}) = \frac{M_{j}}{E_{\text{c.m.}}} \cdot \frac{B_{1}(E_{\text{c.m.}})\sqrt{12\pi[\Gamma_{e^{+}e^{-}}B(D_{s}^{*}D_{s}^{*})]_{j}\Gamma_{j}}}{E_{\text{c.m.}}^{2} - M_{j}^{2} + iM_{j}\Gamma_{j}} \cdot \sqrt{\frac{\beta^{3}(E_{\text{c.m.}})}{\beta^{3}(M_{j})}}$$
(4)

is the *j*th BW amplitude (j = 2, 3), the Blatt-Weisskopf function  $B_1(E_{c.m.}) = \sqrt{1/[1 + q^2(E_{c.m.})R^2]}$  is used as the *P*-wave barrier factor [45,46] with  $q(E_{c.m.})$  the momentum of  $D_s^{\pm}$  and  $R = 1.6 \text{ GeV}^{-1}$  [47] the barrier radius,  $a_1$  is the coefficient for the  $BW_1$ ,  $[\Gamma_{e^+e^-}B(D_s^*D_s^*)]_j$  is the product of the  $e^+e^-$  partial width and the branching fraction of  $D_s^{\pm}D_s^{\pm}$  for the *j*th resonance,  $\beta(E_{c.m.})$  is the velocity of  $D_s^{\pm\pm}$ ,  $a_0$  is the coefficient for the PHSP amplitude, *n* is a free exponent,  $\phi_j$  and  $\phi_0$  are the relative phases. With the fitted line shape, a MC-weighting method [42] is used to iteratively update the efficiencies, the ISR correction factors, the measured dressed cross sections, and the fitted line shape. After four iterations, the fit to the measured dressed cross section converged.

TABLE I. The fitting results of the dressed cross sections.

	Result 1	Result 2	Result 3
$M_1  ({\rm MeV}/c^2)$	$4186.8\pm8.7$	$4194.1\pm 6.8$	$4195.6 \pm 6.5$
$\Gamma_1$ (MeV)	$55\pm15$	$61.1\pm8.5$	$61.7\pm7.7$
$M_2$ (MeV/ $c^2$ )	$4414.6\pm3.4$	$4411.9\pm3.2$	$4411.1 \pm 3.2$
$\Gamma_2$ (MeV)	$122.5\pm7.5$	$120.2\pm7.4$	$119.9\pm7.3$
$M_3$ (MeV/ $c^2$ )	$4793.3\pm6.7$	$4789.7\pm8.7$	$4786.0\pm9.4$
$\Gamma_3$ (MeV)	$27.1\pm6.5$	$42\pm75$	$60\pm34$

The final fit of the dressed cross sections of  $e^+e^- \rightarrow$  $D_s^{*+}D_s^{*-}$  is taken to determine the parameters of the three structures. In the nominal fit of the dressed cross sections, only statistical uncertainties are considered. We find three sets of fitting results with comparable goodness of fit, which are shown in Fig. 2 and Table I. Because of the limited number of data points around 4.79 GeV, the fitted mass of the third structure varies from 4786 to 4793.3 MeV/ $c^2$  and the width from 27.1 to 60 MeV. The statistical significance of the third structure exceeds  $5.9\sigma$  in all three fitting procedures, indicating that incorporating this amplitude leads to a more accurate description of the cross sections compared to using only two BWs. Besides the three BWs, one additional BW is tried to better describe the data points around 4.55 GeV, but it is not kept due to its small statistical significance.

The Born cross sections are obtained by applying the VP correction on the dressed cross sections. The obtained results are summarized in the Supplemental Material [48]. The systematic uncertainties for the measured Born cross sections are described as follows, some of which are common along all the energy points, while others are estimated depending on the  $E_{c.m.}$  range.

The systematic uncertainties of tracking (particle identification) efficiency are estimated to be 0.5% (0.5%) per  $K^{\pm}$  and 0.2% (0.4%) per  $\pi^{\pm}$  with a control sample of  $D_s^{\pm} \rightarrow$  $K^+K^-\pi^{\pm}$  decays [49]; thus a 1.2% (1.4%) systematic uncertainty is assigned for the tracking efficiency (particle identification) in the  $D_s^{\pm} \rightarrow K^+ K^- \pi^{\pm}$  candidates selection. The systematic uncertainty in the efficiency for photon reconstruction is set conservatively to 1% based on a study with a sample of  $J/\psi \rightarrow \rho \pi$  events [50]. From fits of the invariant mass spectrum of  $D_s^{\pm} \rightarrow K^+ K^- \pi^{\pm}$  candidates and of the modified missing mass of  $D_s^{*\pm} \rightarrow \gamma K^+ K^- \pi^{\pm}$  candidates, the efficiencies for signal in the mass window for both data and MC samples can be calculated, and the relative differences in efficiency between data and MC simulation are taken as systematic uncertainties for the  $D_s^{\pm}$ mass window and the modified missing mass window, respectively, which cover the possible resolution difference and the zero width setting for  $D_s^{\pm}$  in MC simulation. The maximum difference in the dressed cross sections between the last two iterations, 0.2%, is taken as the systematic uncertainty for the stability of the iteration results. The systematic uncertainty of the branching fraction for  $D_s^{\pm} \rightarrow$  $K^+K^-\pi^{\pm}$  and  $D_s^{*\pm} \rightarrow \gamma D_s^{\pm}$  is taken from Ref. [35]. The integrated luminosities are measured by OED events [51] with a systematic uncertainty of 1%. The uncertainty from VP correction is 0.1% [41]. The uncertainty of the peaking background subtraction from the  $e^+e^- \rightarrow D_s^{\pm}D_s^{*\mp}$  process is estimated to be 1% mainly from the uncertainties of cross section measurement. Instead of the HELAMP model, the PHSP model [31,32] is also used to generate  $e^+e^- \rightarrow$  $D_s^{*\pm} D_s^{*\mp}$  events and the maximum difference in efficiency, 2.2%, is taken as the systematic uncertainty for the generation model. We get the total common systematic uncertainty by adding them in quadrature, which is 4.0%.

The shape related parameters  $\Delta m$ ,  $\Delta \sigma$ , and  $c_1$  are fixed to the averaged values in the nominal fit (see Fig. 1 for an example). The differences of the fitted signal yields, when these parameters are floating, are within statistical uncertainties. However, to cover these differences conservatively, the whole energy range is divided into three intervals (4.226,4.3), (4.3,4.4), and (4.4,4.95) GeV with assigned systematic uncertainties 2%, 5%, and 2%, respectively, due to the signal and background shapes. The boundaries of the nominal fitting range for  $M_{\gamma KK\pi}$ , which is [2.02, 2.20] GeV/ $c^2$ , are changed by 10 MeV to estimate the corresponding fitting range uncertainties. These are assigned to be 4%, 5%, and 4%, respectively, in the energy intervals (4.226,4.3), (4.3,4.4), and (4.4,4.95) GeV. Equataion (2) is used to fit the data iteratively and get the converged dressed cross sections, during that the cross section line shape is similar to the one in Fig. 2(a). Other two different lineshapes with comparable fitting goodness, that are similar to the results shown in Figs. 2(b) and 2(c), plus an additional lineshape obtained by the LOWESS (LOcally WEighted Scatterplot Smoothing) [52,53], are used to calculate the systematic uncertainties for the lineshape description by repeating the iterations and taking the differences in the results. The systematic uncertainty of the measured  $E_{\rm c.m.}$  is found to be less than 0.8 (0.6 MeV) for  $4.226 < E_{\rm c.m.} < 4.6$  (4.6 <  $E_{\rm c.m.} < 4.95$  GeV) [25–27] and it is used to shift all the energy points to conservatively estimate the impacts on the measured cross sections. Since the cross section lineshape varies dramatically near the threshold, the  $E_{cm}$  uncertainty could have significant impact on the ISR correction factors nearby, subsequently affecting the measured cross sections and the fitting results around the threshold. The MC samples at the first four  $E_{c.m.}$ points near the threshold are regenerated with the shifted energies to update ISR corrections. After the iterations with the shifted energy points and the updated ISR correction factors near threshold, the resulting differences in the Born cross sections are taken as the systematic uncertainties due to the  $E_{\rm c.m.}$  uncertainty. These systematic uncertainties are summarized in Table II by assuming no correlation among different sources.

The sum of three BW amplitudes with the one for the phase-space is an imperfect model, but it is useful to describe the cross section line shape smoothly for the iterative ISR correction procedure and to obtain masses and

Sources	Systematic uncertainties (%)								
Common	4.0								
Energy (interval) (GeV)	4.226	4.228	4.233	4.233 ~ 4.24	4.24 ~ 4.3	4.3 ~ 4.4	4.4 ~ 4.82	4.843	4.86 ~ 4.95
Signal yields fitting with fixed parameters				2.0	5.0			2.0	
Signal yields fitting range Cross section line shape description			5.0	4.0	2.0	5.0 5.0	2.0	4.0 5.0	2.0
$E_{\rm c.m.}$ uncertainty	24.5	20.0	9.4			0.8			
Total	25.7	21.5	12.2	7.9	6.4	9.6	6.4	7.9	6.4

TABLE II. Relative systematic uncertainties of the measured Born cross sections. As the effects and the data statistics are energy dependent, some systematic uncertainties are estimated in several energy intervals combining some datasets with low luminosities.

TABLE III. The systematic uncertainties of the fitted masses and widths. Fitting represent the uncertainty from the multiple fitting results. *R* represent the uncertainty from the barrier radius,  $E_{\rm c.m.}$  the systematic errors from the  $E_{\rm c.m.}$  uncertainty and the  $\sigma_{\rm dressed}$  the systematic uncertainties on the measured dressed cross sections.

Sources	Fitting	R	E <sub>c.m.</sub>	$\sigma_{ m dressed}$	Total
$\overline{M_1 (\mathrm{MeV}/c^2)}$	8.8	2.9	28.3	5.1	30
$\Gamma_1$ (MeV)	6.7	1.9	51	11.8	53
$M_2 ({\rm MeV}/c^2)$	3.5	0.6	4.0	3.0	6.1
$\Gamma_2$ (MeV)	2.6	0.2	7.6	1.0	8.1
$M_3$ (MeV/ $c^2$ )	7.3	1.0	2.4	5.1	9.3
$\Gamma_3$ (MeV)	32.9	1.1	5.3	3.4	34

widths of the resonance(-like) structures for reference. The systematic uncertainties of the fitted masses and widths of the three resonances are listed in Table III. There are three fitting results as listed in Table I with comparable goodness of fit. The fitting result 1 is taken as the nominal one, and the biggest differences in the fitted central values between result 1 and the other two are taken as the systematic uncertainties from the multiple fitting results. The parameter R is changed from 1.6 in the nominal fit to 5 GeV<sup>-1</sup> (corresponds the scale of the strong interaction which is about 1 fm) [47,54], and the variations in the fitting results are taken as the corresponding systematic uncertainties. The uncertainty from the measured  $E_{c.m.}$  has impact not only on the cross sections but also on the fitting results. After the iterations with the shifted energies and the updated ISR correction factors, the differences in the fitting results are considered as the uncertainty from the  $E_{\rm c.m.}$ uncertainty. The systematic uncertainties on the measured dressed cross sections, which are considered as the same as these on the Born cross sections since the uncertainty from VP correction is negligible, consist of a common part and an uncommon part. The common part is the same for all energies and has no effect on fitted masses and widths of the BW functions. The uncommon part is included to redo the cross section fitting and the resulting differences are taken as systematic uncertainties.

In summary, with the world's largest  $e^+e^-$  scan data sample between 4.226 and 4.95 GeV accumulated by BESIII, the Born cross sections of  $e^+e^- \rightarrow D_s^{*+}D_s^{*-}$  are measured precisely. Two enhancements in the  $E_{c.m.}$  dependent cross sections are observed around 4.2 and 4.45 GeV. The  $E_{c.m.}$  dependent cross section lineshape is modeled with a sum of three BW and one PHSP amplitudes. The fitted mass and width for the first resonance are (4186.8 ±  $8.7 \pm 30$ ) MeV/ $c^2$  and (55 ± 15 ± 53) MeV, respectively. These results are consistent with the  $\psi(4160)$ observed in the inclusive cross section of  $e^+e^- \rightarrow$ hadrons [55] and in the dimuon spectrum of  $B^- \rightarrow$  $K^-\mu^+\mu^-$  [56]. While considering the systematic uncertainties, these results are also consistent with  $\psi(4230)$  observed in the  $\pi^+\pi^- J/\psi$  mode. The fitted mass and width for the second resonance are  $(4414.6 \pm 3.4 \pm$ 6.1) MeV/ $c^2$  and (122.5  $\pm$  7.5  $\pm$  8.1) MeV, respectively. The mass is consistent with  $\psi(4415)$ , and the measured width from this work is a bit higher than the world average value of  $\psi(4415)$  [35], but still within three standard deviations. If we assume that this resonance is the  $\psi(4415)$ , this is the first time that this state is observed in the  $D_s^{*+}D_s^{*-}$  decay mode. An additional third BW amplitude describes the  $E_{c.m.}$  dependent cross sections around 4.79 GeV better than just using two BW functions, with statistical significance greater than  $5.9\sigma$ , however, more data points in the vicinity are needed for further clarification [57]. It is out of the scope of this Letter, but a unitary approach based on K-matrix formalism to fit the cross-section results of various exclusive channels is expected to be carried out as a more comprehensive and robust analysis of the vector-charmonium(-like) structures (for instance, an analysis for vector bottomonia with this method can be found in Ref. [58]).

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